

Inference at \* 1  
of proof for Lemma less-fast-fib:

....assertion.... NILNIL

$\vdash \forall n, a, b: \mathbb{N}.$

$\{m: \mathbb{N} \mid$

$\forall k: \mathbb{N}.$

$(a = \text{fib}(k))$

$\Rightarrow ((k \leq 0) \Rightarrow (b = 0))$

$\Rightarrow ((0 < k) \Rightarrow (b = \text{fib}(k - 1)))$

$\Rightarrow (m = \text{fib}(n+k))\}$

by (InductionOnNat)

CollapseTHEN (Auto').

1:

1.  $a : \mathbb{N}$

2.  $b : \mathbb{N}$

$\vdash \{m: \mathbb{N} \mid$

$\forall k: \mathbb{N}.$

$(a = \text{fib}(k))$

$\Rightarrow ((k \leq 0) \Rightarrow (b = 0))$

$\Rightarrow ((0 < k) \Rightarrow (b = \text{fib}(k - 1)))$

$\Rightarrow (m = \text{fib}(0+k))\}$

2:

1.  $n : \mathbb{Z}$

2.  $0 < n$

3.  $\forall a, b: \mathbb{N}.$

$\{m: \mathbb{N} \mid$

$\forall k: \mathbb{N}.$

$(a = \text{fib}(k))$

$\Rightarrow ((k \leq 0) \Rightarrow (b = 0))$

$\Rightarrow ((0 < k) \Rightarrow (b = \text{fib}(k - 1)))$

$\Rightarrow (m = \text{fib}((n - 1)+k))\}$

4.  $a : \mathbb{N}$

5.  $b : \mathbb{N}$

$\vdash \{m: \mathbb{N} \mid$

$\forall k: \mathbb{N}.$

$(a = \text{fib}(k))$

$\Rightarrow ((k \leq 0) \Rightarrow (b = 0))$

$\Rightarrow ((0 < k) \Rightarrow (b = \text{fib}(k - 1)))$

$\Rightarrow (m = \text{fib}(n+k))\}$

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[http://www.nuprl.org/FDLcontent/p0\\_963683\\_/p25\\_528941\\_1.html](http://www.nuprl.org/FDLcontent/p0_963683_/p25_528941_1.html)